

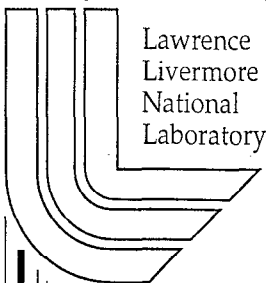
# Stiffness and Strength Properties for Basic Sandwich Material Core Types

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# **STIFFNESS AND STRENGTH PROPERTIES FOR BASIC SANDWICH MATERIAL CORE TYPES**

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## **ABSTRACT**

Three basic core material types for sandwich structure applications are studied. The three two-dimensional pattern types are: honeycomb, triangular cells, and a new configuration involving star type cells. The specific critical properties of stiffness and strength type are identified and studied, both theoretically and experimentally.

## **INTRODUCTION**

Sandwich structures have been used in numerous aspects of aircraft construction as well as in many other applications. Typical sandwich structures are made up of two thin, stiff, strong faces separated by a very lightweight material known as the core. By choosing appropriate core materials based on intended applications, not only are sandwich panels able to achieve high stiffness, and strengths comparable to those of single solid panels, but also great savings in weight.

Many types of low density materials that satisfy the requirements of sandwich structures are used as core materials, and one of the most popular cores is the hexagonal core. This core has a two-dimensional hexagonal pattern made of thin walled structures in one plane. Because cores with two-dimensional patterns such as hexagonal core provide a direct connection between the face panels, they generally show good structural efficiency.

When a material has hexagonal symmetry like a hexagonal core (Figure 1), the stiffness matrix relating stresses and strains has five independent constants. This reveals that the hexagonal core can be considered transversely isotropic and has a plane of isotropy. Gibson and Ashby [1997] have extensively studied the honeycomb form.

A core with a triangular pattern is also isotropic in the plane. One triangle shows only triangular symmetry. However, if six triangles are combined, this pattern has hexagonal symmetry as shown in Figure 1. In other words, this triangular core is isotropic in this plane. Christensen [1995] suggested a new two-dimensional pattern which has six-pointed star-shaped cells adjacent to hexagonal cells. This pattern also has hexagonal symmetry and is isotropic in the plane (Figure 1).

In the current study, the primary objective is to examine and compare the relevant mechanical characteristics of behavior for the three core types having isotropic patterns—the triangular core, the hexagonal core and the starcell core—as related to applications in sandwich structures.

## **Results**

The mechanical characteristics of three types of cores with two-dimensional isotropic patterns—triangular, hexagonal, and starcell—were studied as related to applications in sandwich structures. The Young's modulus, shear modulus, and Poisson's ratio were calculated for the three core types in the direction normal to the faces. The compressive buckling strength and shear buckling strength were calculated for the three core types by modeling each cell wall of the core as a plate under compressive or shear load. To verify this model, tests were conducted on scaled specimens to measure the compressive buckling strength of each core. The bending flexibility's of the three cores were also studied. Compliances for the three cores were measured using flexural tests. Tests were performed on each core type in which the deflection of a circular core sample loaded at its center was measured. The three isotropic core patterns exhibited distinct characteristics, as shown in Figure 2. The results are expressed as a function of the relative density of the core material, and discussed in more detail by Kim and Christensen [1999].

## **REFERENCES**

Gibson, L. J. and Ashby, M., Cellular Solids Structure and Properties, (Cambridge University Press, Cambridge, 1997).

Christensen, R. M., "The hierarchy of microstructures for low density materials," ZAMP 46 (1995) 5506-5521.

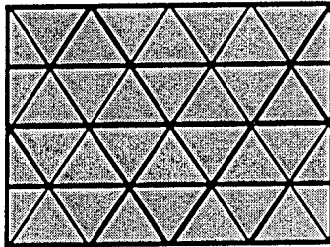
Kim, B. and Christensen, R. M., "Basic Two-Dimensional Core Types for Sandwich Structures," Int. J. Mechanical Sciences, in press.

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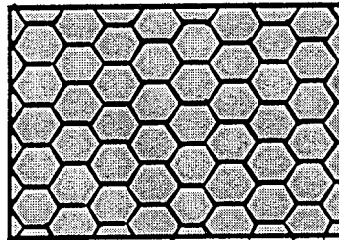
- Objective

Detailed study of three prototype 2-D core forms for sandwich structures

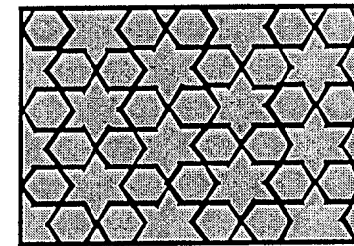
- Basic 2-D Core Forms



Triangular



Hexagonal  
(Honeycomb)



Star  
(New Form)



- Approach

Theoretical and Experimental investigation of three dimensional stiffness and strength properties

- Critical Properties

In-plane moduli, shear  $G$  and bulk  $K$   
Out of plane shear strength

**Figure 1 Patterns**

## Stiffness Theory

	Triangular	Hexagonal	Star
$G/E_m$	$\frac{1}{8} \left( \frac{\rho}{\rho_m} \right)$	$\frac{3}{8} \left( \frac{\rho}{\rho_m} \right)^3$	$\frac{3}{16} \left( \frac{\rho}{\rho_m} \right)^3$
$K/E_m$	$\frac{1}{4} \left( \frac{\rho}{\rho_m} \right)$	$\frac{1}{4} \left( \frac{\rho}{\rho_m} \right)$	$\frac{9}{16} \left( \frac{\rho}{\rho_m} \right)^3$

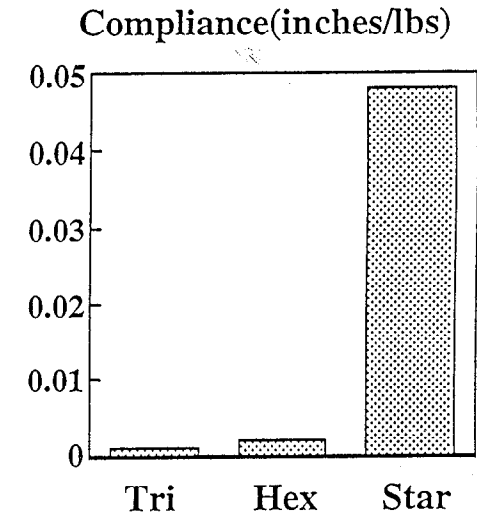
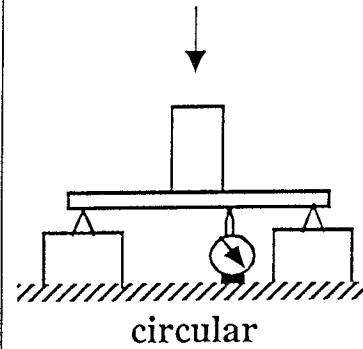
\*  $\rho$  - density

## Compressive Strength, Shear Strength Theory

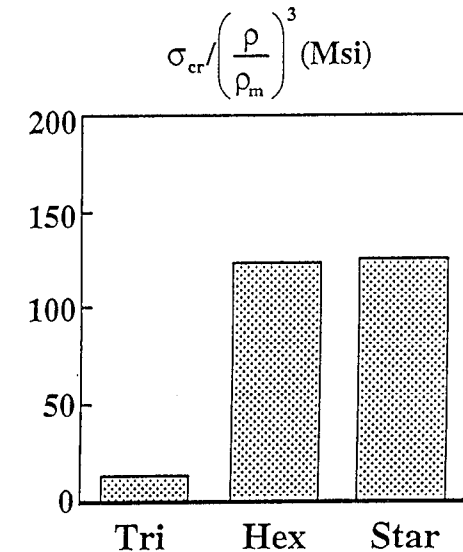
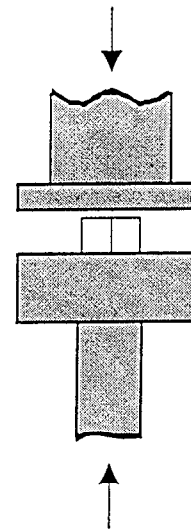
	Triangular	Hexagonal & Star
$\sigma_{cr}$	$\frac{1}{9} \beta_n \frac{E_m}{1-\nu_m^2} \left( \frac{\rho}{\rho_m} \right)^3$	$\beta_n \frac{E_m}{1-\nu_m^2} \left( \frac{\rho}{\rho_m} \right)^3$
$\tau_{cr}$	$\frac{1}{9} \beta_s \frac{E_m}{1-\nu_m^2} \left( \frac{\rho}{\rho_m} \right)^3$	$\beta_s \frac{E_m}{1-\nu_m^2} \left( \frac{\rho}{\rho_m} \right)^3$

\*  $\beta_n, \beta_s$  from boundary conditions

## Stiffness Experiment



## Strength Experiment



**Figure 2 Results**